

$$\bar{x} = \frac{\sum_{i=1}^n x_i}{n} \qquad s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}$$

$$P(A^c) = 1 - P(A) \qquad P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{P(B|A)P(A)}{P(B|A)P(A) + P(B|A^c)P(A^c)}$$

## Discrete Random Variables

Let  $X$  be a discrete random variable with a pmf of  $p(x)$  then

$$E[X] = \sum_x xp(x)$$

Let  $X$  be a random variable, then

$$Var(X) = E[X^2] - E[X]^2$$

Linear combination of random variables  $X$  and  $Y$  and fixed numbers  $a$  and  $b$ :

$$E[aX + bY] = aE[X] + bE[Y]$$

$$Var(aX + bY) = a^2Var(X) + b^2Var(Y)$$

Distribution	pmf	$E(X)$	$Var(X)$
Binomial	$\binom{n}{k} p^k (1-p)^{n-k}$	$np$	$np(1-p)$
Geometric	$(1-p)^{n-1} p$	$\frac{1}{p}$	$\frac{1-p}{p^2}$
Discrete Uniform	$\frac{1}{n}$	$\frac{a+b}{2}$	$\frac{(b-a+1)^2-1}{12}$
Poisson	$\frac{\lambda^k}{k!} e^{-\lambda}$	$\lambda$	$\lambda$

## Continuous Random Variables

$$E[X] = \int_{x \in \Omega_x} xf(x) dx$$